

Effect of Load Impedance on the Performance of Microwave Negative Resistance Oscillators

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Abstract: *In microwave negative resistance oscillators, the RF transistor presents impedance with a negative real part at either of its input or output ports. According to the conventional theory of microwave negative resistance oscillators, in order to sustain oscillation and optimize the output power of the circuit, the magnitude of the negative real part of the input/output impedance should be maximized. This paper discusses the effect of the circuit's load impedance on the input negative resistance and other oscillator performance characteristics in common base microwave oscillators. New closed-form relations for the optimum load impedance that maximizes the magnitude of the input negative resistance have been derived analytically in terms of the Z-parameters of the RF transistor. Furthermore, nonlinear CAD simulation is carried out to show the deviation of the large-signal*

optimum load impedance from its small-signal value. It has been shown also that the optimum load impedance for maximum negative input resistance differs considerably from its value required for maximum output power under large-signal conditions. A 1.8 GHz oscillator circuit has been designed and simulated using a typical SiGe hetero-junction bipolar transistor (HBT) to verify the proposed approach of analysis.

Keywords: Negative Resistance Oscillators, Common Base Oscillator, Microwave Nonlinear Circuits, SiGe HBT Transistors.

1. Introductory Concepts

RF and microwave oscillators are fundamental elements in different wireless communication systems. Basically, there are two approaches for the analysis of RF oscillators: the open-loop gain approach [1, 2] and the negative resistance approach [3, 4].

In the open-loop gain method, the oscillator circuit is viewed to be composed of an amplifier cascaded with a resonator. The open loop gain, S_{21} , of the combination is evaluated and tested across a frequency range around the desired oscillation frequency. The necessary conditions for starting the oscillation is that the phase of S_{21} should equal to zero, while there is a considerable gain margin at the frequency of oscillation [5]. When the loop is closed, the output signal builds until reaching a steady state condition where the gain becomes 0 dB as the RF device enters the nonlinear region. This causes shift in the oscillation frequency and other performance characteristics and therefore the design approach should be modified under large-signal conditions.

On the other hand, in negative resistance oscillators the RF device is characterized as a one-port network by its input impedance Z_{in} and is connected with a resonator of impedance Z_r as

shown in Figure (1). The circuit can oscillate if the resonator's loss is equalized by the negative resistance of the active device.

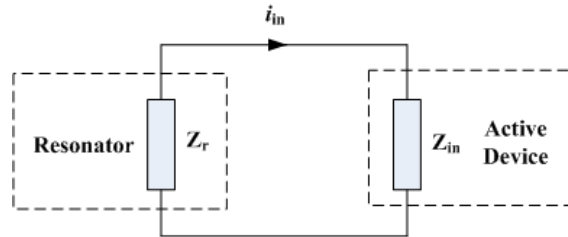


Figure (1): A Simplified Topology of the Negative Resistance Oscillator.

The loop equation of the circuit in Figure (1) can be written as:

$$i_{in} \cdot (Z_{in} + Z_r) = 0 \quad (1)$$

Equation (1) can be satisfied if either $i_{in} = 0$ or $Z_{in} + Z_r = 0$. For an existing current signal at the input of the active device, i_{in} should not equal to zero, and therefore:

$$Z_{in} + Z_r = 0 \quad (2)$$

This means that:

$$Z_r = -Z_{in} \quad (3)$$

or:

$$X_r = -X_{in} \quad (4. a)$$

$$R_r = -R_{in} \quad (4. b)$$

So, at the oscillation frequency the reactance of the resonator should equal the input reactance of the active device in magnitude but with opposite sign. This means that if the input reactance of the active device is capacitive, then the reactance of the resonator should be inductive and vice versa. Similarly, the resistances of the resonator and the active device are equal in magnitude and differ in

sign. But since the resonator is a passive circuit then its resistance is positive in all conditions, and therefore the active device should present a negative resistance at the oscillation frequency.

The input resistance and reactance of the active device are not solely functions of the frequency but vary also with the power level at the input port of the device. So, the large signal magnitude of R_{in} is different from its small signal value due to the inherent nonlinearities in the active device. This resistance usually decreases with power level in most practical RF devices as shown in Figure (2) [6]. In this sketch, the value of the small signal input resistance equals to $-R_o$, while P_{in} represents the available power at the input port, and P_{th} is the threshold input power at which the large-signal device's input resistance deviates from its small-signal value.

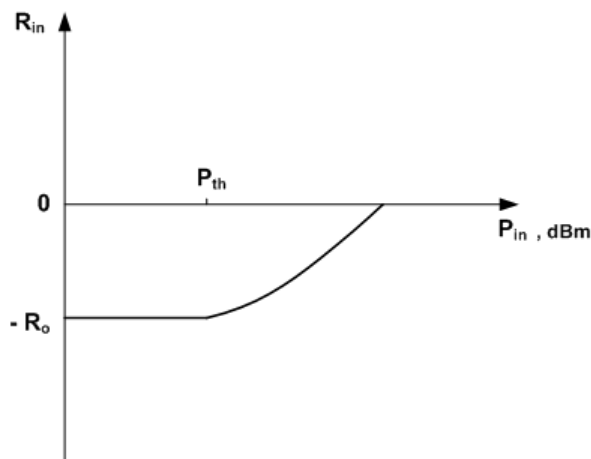


Figure (2): Typical Variation of Negative Input Resistance with Power Level.

So, the necessary condition for oscillation is to make R_r less than the magnitude of the small-signal input resistance in order to place the operating point beyond threshold:

$$R_r < |R_o| \tag{5}$$

The resonator resistance R_r is usually taken equal to $|R_o|/3$ as a practical rule of thumb for the startup of oscillation [6].

2. Related Work

The fundamental concepts of negative resistance microwave oscillators were established by Kurokawa's work [3,7]. He developed the steady state oscillation condition of the oscillator circuit. Further studies were concentrated on the use of large signal S-parameters to maximize the output power and efficiency for microwave oscillators [8-10]. Analytic derivation of the large-signal S-parameters in terms of the input and output device terminal voltage amplitudes was carried out [11]. These equations are formulated systematically as a root finder computer algorithm to determine the circuit elements for maximum oscillator's output power.

Another technique for the evaluation of different oscillator circuit topologies for optimized output power was carried out depending on the measurements of an optimized power amplifier [12]. This technique takes benefits from the ease of power amplifier measurements when compared with oscillator's measurement. A simplified quasi-linear design technique for GaAs MESFET oscillators was also developed [13]. In this approach the generated oscillator's power is derived in terms of the gate and drain RF voltages. The oscillator circuit elements are derived to maximize the generated power under the limiting conditions of the terminal voltage amplitudes.

An analytical approach to the design of microwave oscillators with output power prediction was documented [14]. This design method is mainly concerned with the calculation of the oscillator's network elements using small-signal RF device two-port parameters as the starting point. The oscillator output power is estimated with the aid of the DC bias voltage and current. A linearized design method that maximizes the added power in a two-

port oscillator was verified [15]. In this technique, different network topologies are analyzed for the sake of optimized output power with the RF device modeled through its small-signal parameters.

Andrei Grebennikov proved analytically that maximum output power of the RF oscillator can be obtained by maximizing the negative real part of the output impedance of the RF device, and derived expressions for the optimum circuit elements based on this assumption [16]. This technique was applied both to BJT [17] and FET [18] oscillator circuits. Microstrip resonators were also used in negative resistance microwave oscillator circuits employing either GaAs FET or bipolar devices [19].

Emitter degeneration technique was applied to increase the oscillation frequency and improve the phase noise and tuning range of RF oscillators [20]. The frequency tuning capability of RF oscillators is performed by inserting varactor diodes in the resonator circuits [21].

A method for designing negative resistance RF oscillators based on large-signal measurement setup was verified [22]. In this technique, measurements are performed based on the real-time active load-pull (RTALP) method for the second and third harmonics using a large-signal network analyzer (LSNA). A novel technique was presented to increase the negative resistance and thereby the output power for common collector Colpitts oscillators by means of an inductor [23]. The inductance value is selected to overcome the parasitic capacitances of the collector-base and emitter-base junctions. Another measurement-based design technique for negative resistance microwave oscillators has been proposed [24]. According to this technique, a harmonic-loaded oscillator can be efficiently designed at the specified frequency using a novel multi-harmonic real-time active load-pull technique. Using this methodology, a stable negative resistance RF transistor active circuit is first optimized with the aid of computer simulations around the desired frequency. The optimal second- and third-

harmonic load impedances that achieve maximum output power are then extracted. The loading network of the oscillator can thereby be synthesized to present the measured optimal harmonic impedances at the device's output port.

To overcome the limitations of the small-signal scattering parameters in predicting the performance behavior of RF oscillators under nonlinear conditions, improved analytical expressions based on large-signal X-parameters have been developed for use in transistor oscillator circuit design [25].

In another recent study, it was shown that increasing the magnitude of the negative output resistance of the RF device does not always lead to greater output power [26]. Finally, the stability analysis of negative resistance oscillators has been analyzed based on X-parameters which provide significant behavioral modeling for the circuit under large-signal conditions [27].

3. Potentially Unstable Active Devices

In order to achieve a negative resistance at one of the RF transistor ports, it should be placed in the unstable region. In other words, the RF transistor should be potentially unstable at the desired frequency of oscillation which means that its stability factor, K , is less than one, where K can be expressed in terms of Z-parameters as [28]:

$$K = \frac{2R_{11}R_{22} - \text{Re}[Z_{12}Z_{21}]}{|Z_{12}Z_{21}|} \quad (6)$$

Where: $R_{11} = \text{Re}[Z_{11}]$, $R_{22} = \text{Re}[Z_{22}]$, and Z_{ij} are the Z-parameters of the RF transistor at the specific frequency.

The oscillation susceptibility of the RF transistor can be increased by connecting it in common base configuration. The instability region of the common base configuration can further be extended by adding an additional feedback element as illustrated in

Figure (3), where an inductor is inserted in the base terminal to constitute a series feedback network [29]. The inductance value can either be calculated analytically using a simplified equivalent circuit model for the RF device, or can be optimized using a microwave CAD simulator. The load stability circle of the RF transistor is first sketched on the Smith chart to view the unstable region for all possible load reflection coefficient values. If the stability circle does not cover a considerable part of the Smith chart, then the circuit presented in Figure (3) should be selected to extend the unstable region.

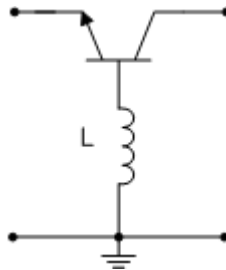


Figure (3): Common Base Configurations with Series Base Inductance.

4. Analytic Determination of the Optimum Load Impedance

A block diagram for the negative resistance oscillator is presented in Figure (4). It consists of an active device with certain positive feedback and is terminated by the resonator at its input port, and a load at its output port. The output matching network is necessary to present the required load impedance Z_L at the output port. The loading effect at the output port greatly affects the value of the input impedance Z_{in} . In order to make the circuit oscillate, the real part of the input impedance should be made negative. To obtain maximum power at the load terminal, the magnitude of the negative input resistance of the RF device is maximized [16]. So,

the optimum load impedance $Z_{L(opt)}$ can be selected to maximize the magnitude of the negative real part of the input impedance.

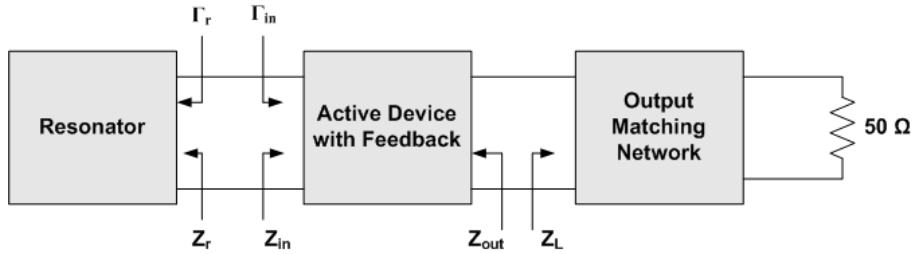


Figure (4): A Block Diagram for the Negative Resistance Oscillator.

It is convenient to analytically determine $Z_L=R_L+jX_L$ which is required to make $|R_{in}|$ maximum. This can be done by evaluating an equation for R_{in} and partial differentiating it with respect to R_L and X_L respectively after characterizing the active device with its Z-parameters at the required frequency.

From two-port network theory, if the device is described in terms of its Z-parameters then the input impedance is given by:

$$Z_{in} = Z_{11} - \frac{Z_{12} \cdot Z_{21}}{Z_{22} + Z_L} \tag{7}$$

After some arrangement,

$$Z_{in} = \frac{Z_{11} \cdot Z_L + \Delta_z}{Z_{22} + Z_L} \tag{8}$$

where:

$$\Delta_z = Z_{11} \cdot Z_{22} - Z_{12} \cdot Z_{21} \tag{9}$$

Equation (8) can be re-written as:

$$Z_{in} = \frac{(R_{11} + jX_{11})(R_L + jX_L) + (R_{11} + jX_{11})(R_{22} + jX_{22}) - (R_{12} + jX_{12})(R_{21} + jX_{21})}{R_{22} + jX_{22} + R_L + jX_L} \quad (10)$$

Where: $Z_{ij}=R_{ij}+jX_{ij}$ are the Z-parameters of the RF transistor at the desired frequency, and $Z_L=R_L+jX_L$ is the load impedance.

Equation (10) should be re-arranged to split the real and imaginary parts where:

$$R_{in} = Re[Z_{in}] \quad (11.a)$$

$$X_{in} = Im[Z_{in}] \quad (11.b)$$

Equation (11.a) can be partially differentiated with respect to R_L and X_L respectively to get the optimum load impedance for maximum negative resistance at the input port:

$$\frac{\partial R_{in}}{\partial R_L} = 0 \quad (12.a)$$

$$\frac{\partial R_{in}}{\partial X_L} = 0 \quad (12.b)$$

In order to differentiate equation (11.a) with respect to R_L , it can be re-written in the form:

$$R_{in} = \frac{N_1}{D_1} \quad (13)$$

The denominator of equation (13) is given by:

$$D_1 = (R_{22} + R_L)^2 + (X_{22} + X_L)^2 \quad (14)$$

And the numerator is arranged as:

$$N_1 = 2 R_{11}R_{22}R_L + R_{11}R_L^2 + X_{12}X_{21}R_L - R_{12}R_{21}R_L + A_1 \quad (15)$$

Where A_1 is given by:

$$A_1 = R_{11}R_{22}^2 - R_{12}R_{21}R_{22} + 2R_{11}X_{22}X_L + R_{11}X_{22}^2 + R_{11}X_L^2 - R_{12}X_{21}X_{22} - R_{12}X_{21}X_L - R_{21}X_{12}X_{22} - R_{21}X_{12}X_L + R_{22}X_{12}X_{21} \quad (16)$$

Applying equation (12.a) and rearranging yields:

$$R_{L(opt)} = \frac{-\alpha_2 + \sqrt{\alpha_2^2 - 4\alpha_1\alpha_3}}{2\alpha_1} \quad (17)$$

where:

$$\alpha_1 = 2R_{11}R_{22} + 2R_{12}R_{21} - 2X_{12}X_{21} + A_3 \quad (18)$$

$$\alpha_2 = 2R_{12}R_{21}R_{22} - 4R_{11}R_{22}^2 - 2R_{22}X_{12}X_{21} + 2R_{11}A_2 + 2R_{22}A_3 - 2A_1 \quad (19)$$

$$\alpha_3 = A_2A_3 - 2R_{22}A_1 \quad (20)$$

$$A_2 = R_{22}^2 + X_{22}^2 + 2X_{22}X_L + X_L^2 \quad (21)$$

$$A_3 = 2R_{11}R_{22} - R_{12}R_{21} + X_{12}X_{21} \quad (22)$$

Equation (17) is derived in terms of the transistor Z-parameters and the load reactance X_L .

Similarly, in order to differentiate equation (11.a) with respect to X_L , it can be re-written in the form:

$$R_{in} = \frac{N_2}{D_2} \quad (23)$$

The denominator of equation (23) is given by:

$$D_2 = (R_{22} + R_L)^2 + (X_{22} + X_L)^2 \quad (24)$$

and the numerator is arranged as:

$$N_2 = 2R_{11}X_{22}X_L + R_{11}X_L^2 - R_{12}X_{21}X_L - R_{21}X_{12}X_L + B_1 \quad (25)$$

Where B_1 is given by:

$$B_1 = 2R_{11}R_{22}R_L + R_{11}R_{22}^2 + R_{11}R_L^2 - R_{12}R_{21}R_{22} - R_{12}R_{21}R_L - R_{12}X_{21}X_{22} - R_{21}X_{12}X_{22} + R_{22}X_{12}X_{21} + R_LX_{12}X_{21} \quad (26)$$

Applying equation (12.b) and rearranging leads to:

$$X_{L(opt)} = \frac{-\beta_2 + \sqrt{\beta_2^2 - 4\beta_1\beta_3}}{2\beta_1} \quad (27)$$

where:

$$\beta_1 = 2R_{12}X_{21} - 2R_{11}X_{22} - 2R_{21}X_{12} + B_3 \quad (28)$$

$$\beta_2 = 2R_{11}B_2 - 4R_{11}X_{22}^2 + 2R_{12}X_{21}X_{22} + 2R_{21}X_{12}X_{22} + 2X_{22}B_3 - 2B_1 \quad (29)$$

$$\beta_3 = B_2B_3 - 2B_1X_{22} \quad (30)$$

$$B_2 = R_{22}^2 + 2R_{22}R_L + R_L^2 + X_{22}^2 \quad (31)$$

$$B_3 = 2R_{11}X_{22} - R_{12}X_{21} - R_{21}X_{12} \quad (32)$$

The real part of the input impedance (R_{in}) can be calculated either from equation (13) or (23), while the imaginary part of the input impedance (X_{in}) can be evaluated in terms of $R_{L(opt)}$ and $X_{L(opt)}$ where:

$$X_{in} = \frac{N_3}{D_3} \quad (33)$$

where:

$$D_3 = (R_{22} + R_L)^2 + (X_{22} + X_L)^2 \quad (34)$$

and

$$N_3 = 2R_{22}R_LX_{11} + R_{22}^2X_{11} + R_{12}R_{21}X_{22} + R_{12}R_{21}X_L - R_{12}R_{22}X_{21} - R_{21}R_{22}X_{12} - R_{12}R_LX_{21} - R_{21}R_LX_{12} + R_L^2X_{11} + 2X_{11}X_{22}X_L + X_{11}X_{22}^2 + X_{11}X_L^2 - X_{12}X_{21}X_{22} - X_{12}X_{21}X_L \quad (35)$$

The derived equations for $R_{L(opt)}$ and $X_{L(opt)}$ apply for small-signal power levels before threshold. But in practice since R_{in} is a function of signal level as depicted in Figure (2), the optimum load resistance $R_{L(opt)}$ and optimum load reactance $X_{L(opt)}$ may vary with power level. $R_{L(opt)}$ and $X_{L(opt)}$ can thus be found from large-signal simulation of the circuit at the desired oscillator's power level and frequency using the non-linear model of the transistor to generate a family of curves for R_{in} , $|\Gamma_{in}|$, power gain, and output power as functions of both R_L and X_L . A compromise is to be done for important oscillator performance characteristics such as high output power, low harmonic distortion, minimal stability factor, and high resonator's quality factor when selecting R_L and X_L from the generated curves.

5. Design of a 1.8 GHz Oscillator Circuit

A microwave oscillator circuit is to be designed and simulated in order to verify the effect of load impedance on its performance characteristics. This circuit operates at the standard 1800 MHz mobile communication band (GSM-1800). Desired specifications are to achieve an output power of more than 10 dBm, second harmonic distortion level better than -20 dBc, and low phase noise at 1.8 GHz.

5.1 Selection of the RF Transistor

SiGe heterojunction bipolar transistors (HBTs) are improved versions of BJT transistors with superior high frequency performance characteristics. The structure is similar to that of the silicon transistor but the base region is incorporated with germanium. The addition of germanium to the base region reduces its resistance and transit time, which increases the transition frequency f_T [30]. The higher base doping concentration reduces also the noise figure of the transistor [31].

In this design, the NPN SiGe heterojunction bipolar transistor NESG2101M05 of Renesas (Previously NEC) has been

selected. This device is a low power transistor and has low noise figure in the order of 0.9 dB at 2 GHz with an associated power gain of 13 dB. It has a typical transition frequency f_T of 17 GHz. The transistor is to be biased at $V_{CE} = 3$ V and $I_C = 20$ mA. The DC simulation of the large-signal model of the transistor indicates that $V_{BE} = 0.835$ V for a collector current of 20 mA with a DC current gain, h_{FE} , of 185.

5.2 Large Signal Z-Parameters and Stability Evaluation

The test circuit for viewing the stability conditions and extracting the large-signal device parameters is shown in Figure (5). The transistor is connected in common base configuration, and a bias circuit is designed to place the Q-point at $V_{CE} = 3$ V and $I_C = 20$ mA. The input power level is varied from -20 dBm to +15 dBm and the simulation frequency is set at 1.8 GHz. The circuit has been simulated using the harmonic balance algorithm provided by the nonlinear microwave CAD program ADS 2009 of Keysight Technologies.

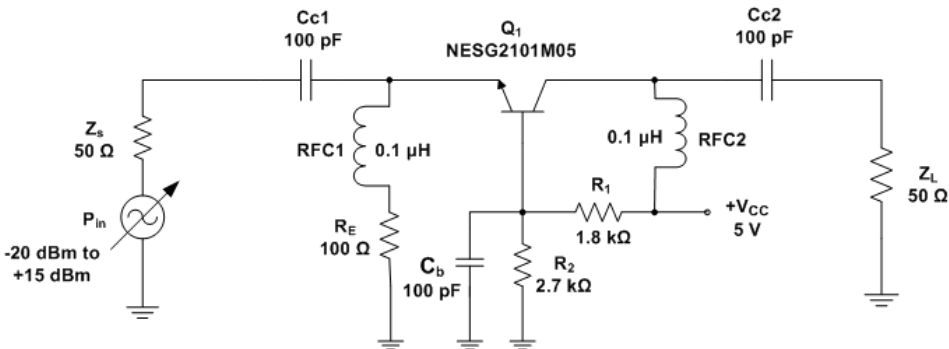


Figure (5): Simulation Setup for Large Signal Z-Parameters Extraction.

The load stability circle is sketched in Figure (6) and is measured at a small-signal input power level of -20 dBm, while Figure (7) presents the stability factor, K , versus input power. As shown from Figure (6), the stability circle covers a large portion of

the Smith chart including the center point and therefore there is no need to add any feedback element for extending the instability region. It could be seen also that this circle encloses most of the upper part of the Smith chart which means that the load impedance is generally an inductive one. The stability factor presented in Figure (7) is less than one for all input power swept values which reveals that the device is potentially unstable at 1.8 GHz for all power levels at the input port.

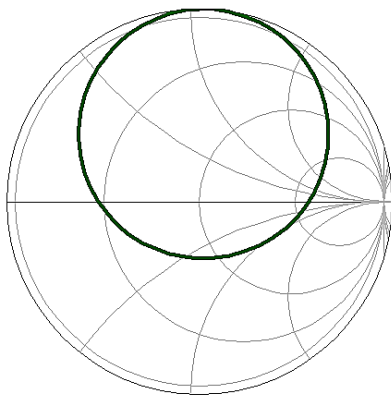


Figure (6): Load Stability Circle at Small Power Level ($P_{in} = -20$ dBm).

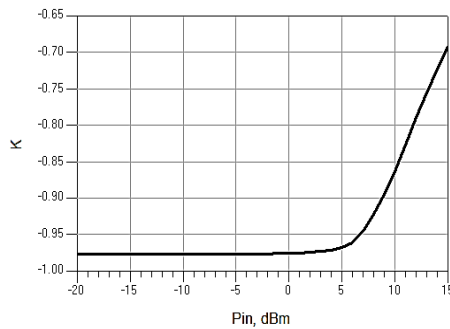


Figure (7): Stability Factor versus Input Power.

The simulated large-signal Z-parameters of the RF transistor are sketched in Figure (8) versus input power. These parameters have been obtained from the large-signal S-parameters test of ADS and applying the S- to Z-parameter conversion relations. It is shown that these simulated parameters start to deviate from their small-signal values after an input power level of 0 dBm approximately. In practice, the large-signal S-parameters can be measured with the aid of modern non-linear vector network analyzers that handle high power levels.

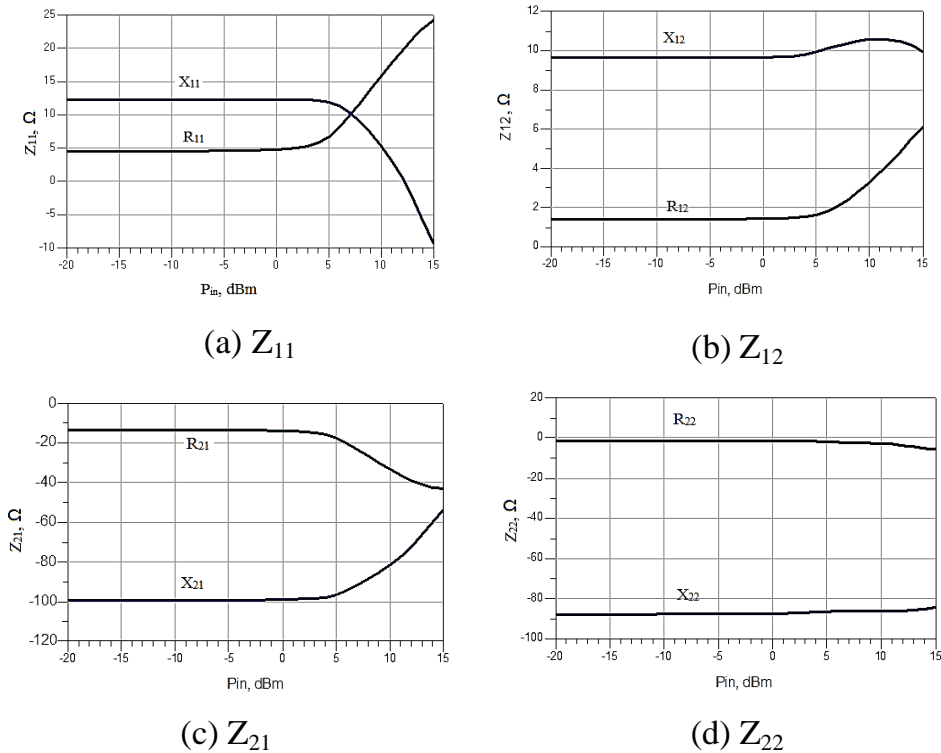
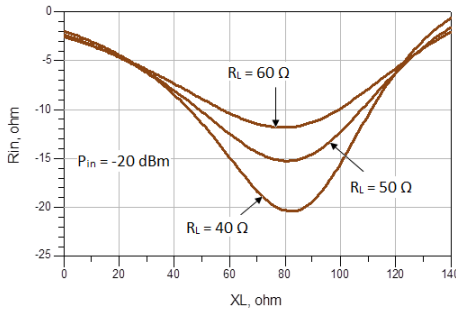


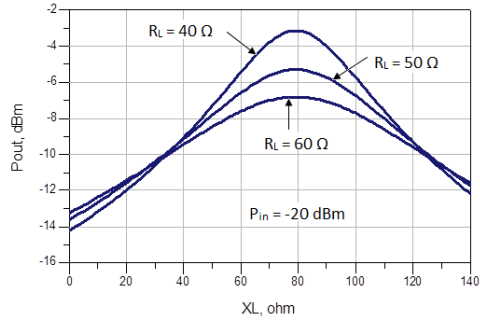
Figure (8): Large Signal Z-parameters of the RF Transistor.

5.3 Simulation of Load Impedance Variations

In order to simulate the effect of the load impedance on the negative input resistance and output power of the oscillator, the simulation setup of Figure (5) has been modified by maintaining the input power level at a certain value and changing the load impedance Z_L , where $Z_L = R_L + jX_L$. Figure (9-a) presents the variation of the input resistance of the RF device with load reactance X_L for three values of R_L with input power of -20 dBm (small-signal condition), while Figure (9-b) shows the equivalent variation of the output power with X_L .



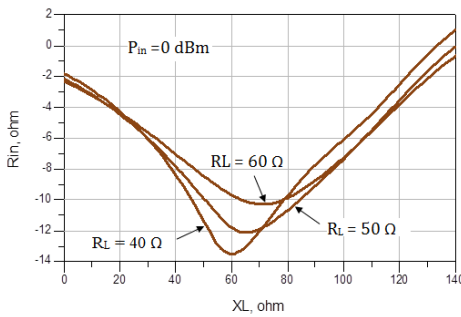
(a) R_{in} versus X_L



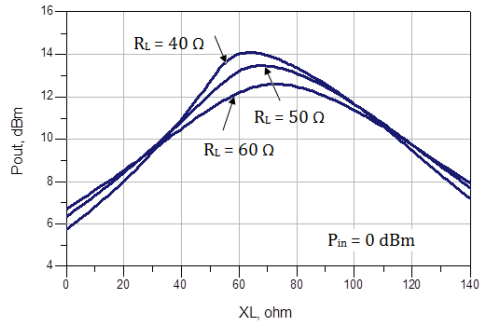
(b) P_{out} versus X_L

Figure (9): Variation of Input Resistance (a) and Output Power (b) versus Load Reactance for Three Different Values of R_L when $P_{in} = -20$ dBm.

In Figure 10, the variations of R_{in} and P_{out} with X_L are sketched with $P_{in} = 0$ dBm (large-signal condition), while Figure 11 presents the corresponding variations for $P_{in} = 3$ dBm (very large-signal condition).



(a) R_{in} versus X_L



(b) P_{out} versus X_L

Figure (10): Variation of Input Resistance (a) and Output Power (b) versus Load Reactance for Three Different Values of R_L when $P_{in} = 0$ dBm.

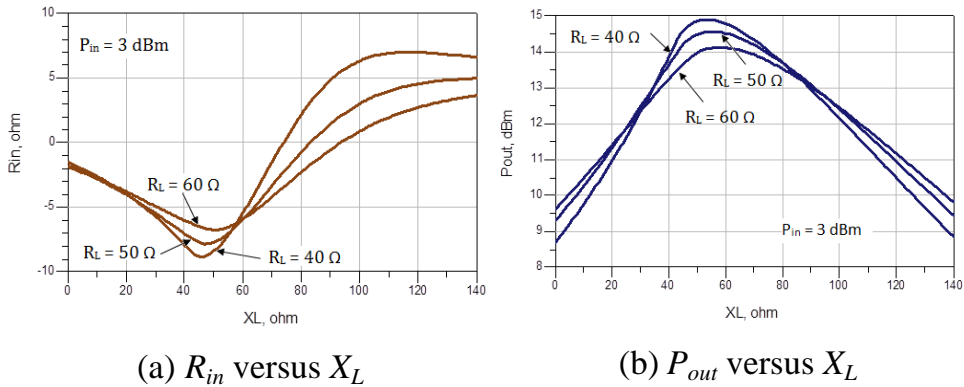


Figure (11): Variation of Input Resistance (a) and Output Power (b) versus Load Reactance for Three Different Values of R_L when $P_{in} = 3 \text{ dBm}$.

From the above curves it can be shown that the optimum load reactance is dependent on the load resistance R_L and the power level at the input port. For example, $X_{L(opt)}$ is around 80Ω when $P_{in} = -20 \text{ dBm}$ and $R_L = 40 \Omega$, and is reduced to 60Ω for $P_{in} = 0 \text{ dBm}$ and $R_L = 40 \Omega$, while it shifts to less than 50Ω for $P_{in} = +3 \text{ dBm}$ and $R_L = 40 \Omega$. It can be seen also that the optimum load reactance for maximum negative input resistance differs slightly from its value required for maximum output power. This difference extends as the input power level is increased due to the increasing effect of the nonlinearities in the active device.

To compare the analytical calculations with the simulated results for the small signal condition ($P_{in} = -20 \text{ dBm}$), the Z-parameters of the RF transistor have been taken from Figure (8) for $P_{in} = -20 \text{ dBm}$. In this case, $Z_{11} = 4.537 + j12.289 \Omega$, $Z_{12} = 1.419 + j9.613 \Omega$, $Z_{21} = -13.382 - j99.355 \Omega$, and $Z_{22} = -1.717 - j87.625 \Omega$. The optimum load reactance, $X_{L(opt)}$, is calculated from equation (27) for the case where $R_L = 40 \Omega$. Table (1) shows a comparison between the calculated and simulated values.

Table (1): Calculated and Simulated Values of $X_{L(opt)}$ and Z_{in} for $R_L = 40 \Omega$.

Parameter	Calculated Value (Small-Signal)	Simulated Value for $P_{in} = -20$ dBm	Simulated Value for $P_{in} = 0$ dBm	Simulated Value for $P_{in} = +3$ dBm
$X_{L(opt)}, \Omega$	82.22	82	60	46
R_{in}, Ω	-20.14	-20.39	-13.47	-8.83
X_{in}, Ω	15.81	15.70	7.84	4.91

As shown from Table (1), the calculated value of $X_{L(opt)}$ is very close to the simulated value for the small-signal condition ($P_{in} = -20$ dBm). However, as power level is increased, the optimum load reactance deviates considerably from its small-signal calculated value. This means that for a successful oscillator design, the optimum load impedance must be chosen specifically for the specified output power level and the corresponding power level at the input port. Similarly, the negative input resistance and output power can be varied with R_L for a given value of X_L . Figure (12) shows this variation for a small-signal input power level of -20 dBm and three different values of X_L . The optimum load resistance required to obtain maximum negative input resistance is around 15 Ω for $X_L = 70 \Omega$ as depicted from Figure (12-a), while its value is about 19 Ω for maximum output power with $X_L = 70 \Omega$. It is clear from Figure (9) that the optimum load reactance for this input power level is about 80 Ω . So, the optimum load impedance for this power level is thus $Z_L = 19+j80 \Omega$.

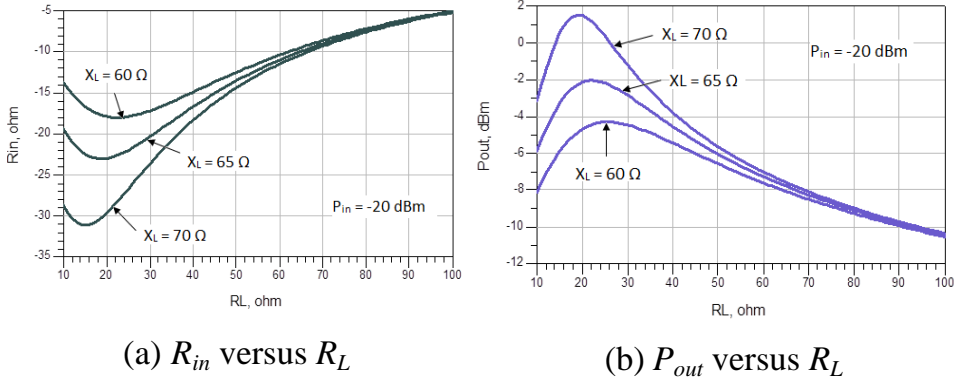


Figure (12): Variation of Input Resistance (a) and Output Power (b) versus Load Resistance for Three Different Values of X_L when $P_{in} = -20$ dBm.

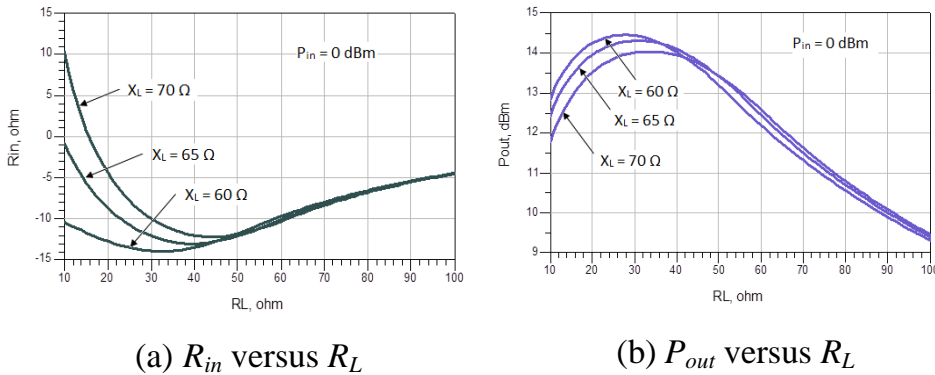
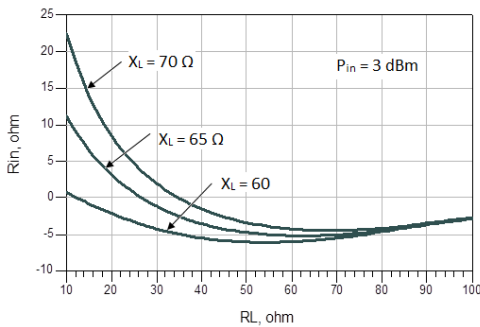


Figure (13): Variation of Input Resistance (a) and Output Power (b) versus Load Resistance for Three Different Values of X_L when $P_{in} = 0$ dBm.

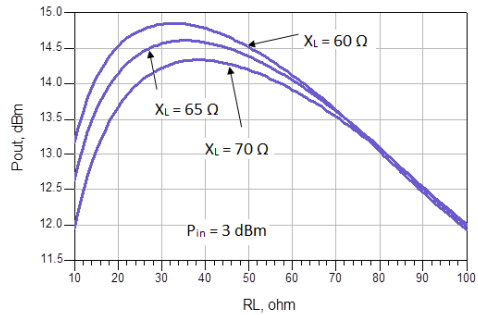
In Figure (13), R_{in} and P_{out} are sketched versus R_L for different values of X_L with increasing the input power level to 0 dBm. It is noticed that there is a considerable change from the results obtained for the small signal simulation in Figure (12). The optimum load resistance for maximum R_{in} is about 32 Ω with $X_L = 60 \Omega$. Its value is reduced to 28 Ω for maximum P_{out} . From Figure (10), it was found that the optimum load reactance is about 60 Ω . So, the optimum load impedance for a maximum power level is Z_L

= $28+j60 \Omega$, and the maximum attainable power in this case is about 14.5 dBm given that $P_{in} = 0$ dBm.

In Figure (14), the simulations are repeated for $P_{in} = 3$ dBm. It is noticed that the optimum load resistance is increased, while the magnitude of the negative input resistance is significantly decreased. The maximum attainable power in this case becomes about 14.85 dBm which is not far away from the value obtained under the condition of $P_{in} = 0$ dBm. This means that the RF device enters saturation at this power level which may increase the distortion level in the output signal.



(a) R_{in} versus R_L



(b) P_{out} versus R_L

Figure (14): Variation of Input Resistance (a) and Output Power (b) versus Load Resistance for Three Different Values of X_L when $P_{in} = 3$ dBm.

Table (2) summarizes the variation in the optimum load resistance with power level for $X_L = 60 \Omega$. The optimum load resistance and input impedance differ significantly for large-signal levels when compared with their small-signal calculated values.

Table (2): Calculated and Simulated Values of $R_{L(opt)}$ and Z_{in} for $X_L = 60 \Omega$.

Parameter	Calculated Value (Small-Signal)	Simulated Value for $P_{in} = -20$ dBm	Simulated Value for $P_{in} = 0$ dBm	Simulated Value for $P_{in} = +3$ dBm
$R_{L(opt)}, \Omega$	22.77	22	32	54
R_{in}, Ω	-17.97	-17.99	-13.93	-6.01
X_{in}, Ω	-4.44	-5.06	6.53	10.99

5.4 Design of the Output Matching and Resonator Networks

Based on the previous simulation results, the optimum load impedance for a maximum output power of 14.5 dBm and an input power level of 0 dBm is selected to be $Z_{L(opt)} = 28+j60 \Omega$. With the circuit terminated with $Z_{L(opt)}$, the input power is swept to view the variation of Z_{in} and P_{out} against input power level as depicted in Figures (15) and (16) below.

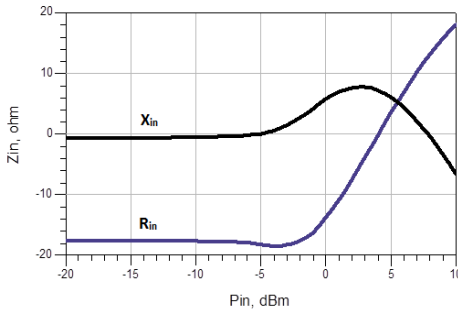


Figure (15): Variation of Z_{in} with Power Level.

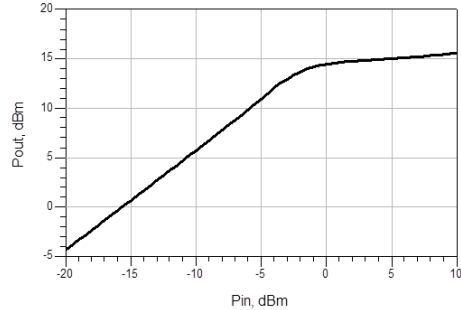


Figure (16): Output Power versus Input Power.

As shown from Figure (15), the small signal negative input resistance equals to -17.5Ω , and changes to -13.77Ω when $P_{in} = 0$ dBm. At this power level, the input reactance, X_{in} , is 5.8Ω . Hence, the resonator impedance $Z_r = 13.77 - j5.8 \Omega$ according to equation (3). Note that the variation of R_{in} against power level in Figure (15)

is typically similar to that of Figure (2). At $P_{in} = 0$ dBm, the output power is 14.5 dBm, and the RF device is operating at the edge of, but not deeply in, the saturation region as shown in Figure (16).

Accordingly, the output matching network of the oscillator is designed with the aid of the Smith chart to transform the 50Ω terminal impedance into $Z_{L(opt)}$ and consists of a short-circuited parallel stub with a series transmission line section as shown in Figure (17). On the other hand, the resonator network is designed to present Z_r at the transistor's input port and consists of a parallel open-ended stub with a series transmission line section as presented in Figure (18).

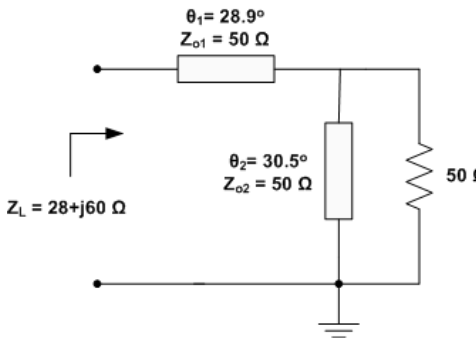


Figure (17): The Output Matching Network of the Oscillator.

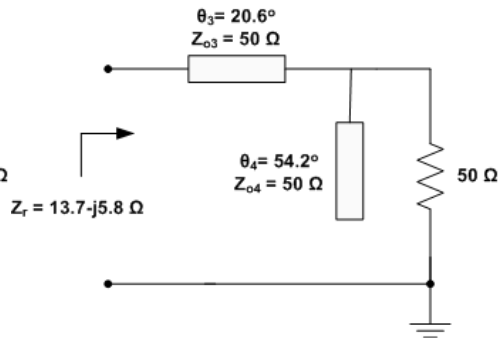


Figure (18): Resonator Network.

5.5 Performance Evaluation of the Oscillator Circuit

The schematic diagram of the final oscillator circuit is presented in Figure (19). As shown from this figure, the transmission line sections were implemented using Microstrip lines. The selected Microstrip substrate type is the low cost epoxy-glass (FR-4) which has a relative dielectric constant ϵ_r of 4.5 and thickness $h = 1.6$ mm. The tangent loss of this substrate is about 0.01, while the conductor thickness $t = 0.05$ mm. The ideal transmission line sections were converted into Microstrip lines using the *Linecalc* tool provided

with the computer program ADS 2009. The lengths and widths of the Microstrip lines were tuned for practical purposes.

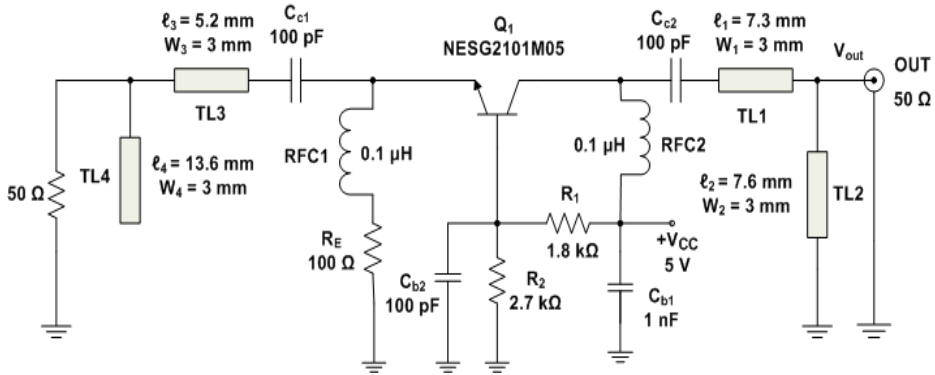


Figure (19): Schematic Diagram for the Final Oscillator Circuit.

The circuit was simulated using the harmonic balance simulator of ADS. In Figure (20), the generated output signal is displayed in time domain, while its power spectrum is sketched in Figure (21). The frequency of the output signal is 1.801 GHz, and the power of the fundamental signal component is 14.32 dBm. The second harmonic level in the output signal is about 24 dBc below the fundamental component, but the third harmonic component is higher, reaching to about 22 dBc as depicted in Figure (21).

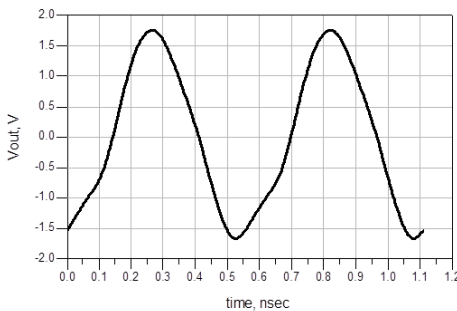


Figure (20): Output Signal of the Oscillator.

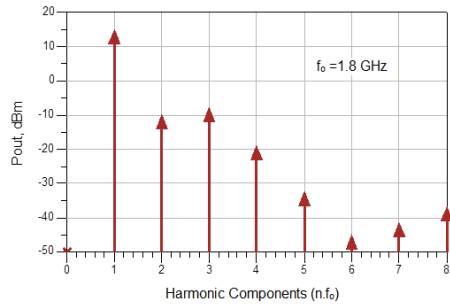


Figure (21): Power Spectrum of the Output Signal.

Figure (22) presents the collector-to-emitter voltage, v_{ce} , in time domain. As shown from this sketch, the RF transistor is not heavily

driven into saturation. In Figure (23), the phase noise of the oscillator is sketched and is about -108 dBc/Hz at an offset frequency of 100 kHz from the carrier.

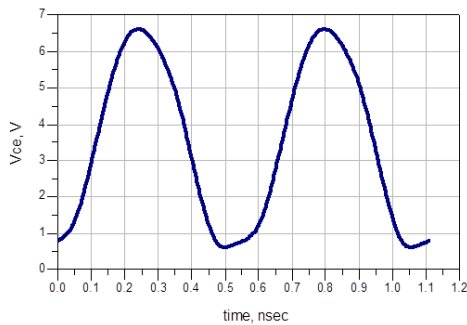


Figure (22): Collector-to-Emitter Voltage.

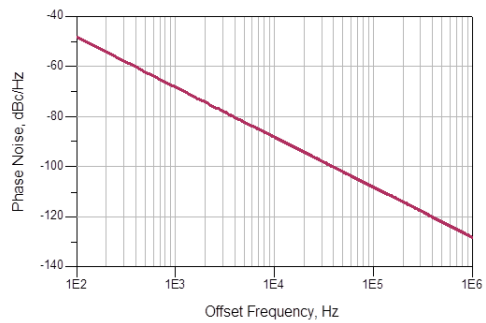


Figure (23): Simulated Phase Noise of the Circuit.

6. Conclusion

The effect of load impedance on the performance characteristics of negative resistance microwave oscillators has been studied thoroughly in this paper. Analytic expressions have been derived for the optimum load impedance in terms of the small signal Z-parameters of the RF transistor. These relations are convenient as an initial guess for the RF oscillator design prior to computer optimization. Throughout computer simulation, it was shown that the optimum load resistance and reactance are dependent on each other. The optimum load impedance varies also with the signal power level at which the active device is operating with. Hence, the load and input impedances of the RF transistor should be extracted at the specific power level for a successful large-signal oscillator design. Furthermore, it was shown that the optimum load impedance for maximum negative input resistance does not coincide with its value required for maximum output power. This difference usually extends as the signal level becomes

larger. The shift between the two values may probably change from device to device.

A 1.8 GHz grounded-base oscillator circuit was designed and simulated with the aid of the microwave CAD program ADS 2009 to confirm the approach of analysis. This circuit is based on a SiGe HBT transistor and generates an RF signal at 1.8 GHz with an output power level of more than 14 dBm, and produces a phase noise of -108 dBc/Hz at an offset frequency of 100 kHz from the frequency of oscillation.

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تأثير ممانعة الحمل على أداء مذبذبات الموجات المايكروية ذات المقاومة السالبة

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المستخلص:

في مذبذبات الموجات المايكروية ذات المقاومة السالبة يكون الجزء الحقيقي لممانعة منفذ الدخل أو الخرج للترانزستور الراديوي سالباً. وبالعودة إلى النظرية التقليدية لتحليل المذبذبات الراديوية ذات المقاومة السالبة فإنه لأجل تحقيق شرط التذبذب مع الحصول على أقصى قدرة خرج من الدائرة فإن مقدار الجزء الحقيقي السالب لممانعة الدخل أو الخرج يتم جعله أقصى ما يمكن.

يناقش هذا البحث تأثير ممانعة الحمل للدائرة على قيمة مقاومة الدخل السالبة وخصائص أداء المذبذب الأخرى. وقد تم اشتقاق معادلات جديدة لاستخراج قيمة ممانعة الحمل المثلى لدائرة المذبذب ذو القاعدة المشتركة بدلالة معاملات الممانعة للترانزستور الراديوي وذلك لتحقيق أعلى قيمة لمقاومة الدخل السالبة. بالإضافة إلى ذلك تم استخدام برامج التصميم المعزز بالحاسوب للاخطية لتتبع التغير بقيمة ممانعة الحمل المثلى في حالة الإشارات ذات السعة العالية عن قيمتها المحسوبة في حالة الإشارات ذات السعة الصغيرة.

وقد لوحظ بأن قيمة ممانعة الحمل المثلى اللازمة لتحقيق أعلى مقاومة دخل سالبة تختلف ألى حدٍ ما عن قيمتها اللازمة لتحقيق أقصى قدرة خرج من الدائرة في حالة الإشارات ذات السعة العالية. وقد تم تصميم ومحاكاة دائرة مذبذب راديوي تعمل في

التردد 1.8 GHz وباستخدام ترانزستور عالي المواصفات من النوع ثنائي القطب ذو
الوصلة غير المتجانسة (SiGe HBT) لتأكيد طريقة التحليل.
الكلمات الرئيسية: مذبذبات المقاومة السالبة، مذبذب القاعدة المشتركة، الدوائر
الميكروية اللاخطية، الترانزستورات ثنائية القطب ذات الوصلة غير المتجانسة.